

Mark Scheme (Results)

Summer 2015

Pearson Edexcel International GCSE Mathematics B (4MB0) Paper 02

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded.
 Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.

 Examiners should also be prepared to award zero marks if the
 - candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

Types of mark

- o M marks: method marks
- o A marks: accuracy marks
- B marks: unconditional accuracy marks (independent of M marks)

Abbreviations

- o cao correct answer only
- o ft follow through
- o isw ignore subsequent working
- o SC special case
- o oe or equivalent (and appropriate)
- o dep dependent
- o indep independent
- o eeoo each error or omission
- awrt -answer which rounds to

No working

If no working is shown then correct answers normally score full marks

If no working is shown then incorrect (even though nearly correct) answers score no marks.

With working

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

Any case of suspected misread loses A (and B) marks on that part, but can gain the M marks.

If working is crossed out and still legible, then it should be given any appropriate marks, as long as it has not been replaced by alternative work.

If there is a choice of methods shown, then no marks should be awarded, unless the answer on the answer line makes clear the method that has been used.

If there is no answer on the answer line then check the working for an obvious answer.

• Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eq algebra.

Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded in another.

Question	Working		Answer	Mark		Notes
1 (a)	1.20×£1400 - €1230				M1	
				2		
			(€)450		A1	
(b)	"€450"× $\frac{75}{100}$ "€450"	" (=£375.00)			M1	oe
	100 1.2					
	(=€337.50)			3		
	"337.50" 75	775 0011			M1	dep
	${1.20}$ ${100}$	375.00"				_
			(£)281.25		A1	
					·	Total 5 marks

Qı	iestion	Working	Answer	Mark		Notes
2	(a)		p + m = 100	1	B1	
	(b)		p - m = 22	1	B1 oe	
	(c)				M1	
		Note: A correct attempt to eliminate either m or p from their equations.				
			p = 61 or $m = 39$ or	3	A1	
			p = 61 or $m = 39$ or $p'' + m'' = 100$			
			p = 61 and $m = 39$		A1	
						Total 5 marks

Question	Working	Answer	Mark	Notes
3	2(x-2) - 3x = 5x(x-2)			M1
	Note: removing denominators allowing one arithmetic slip			
		$5x^2 - 9x + 4(=0)$ (o.e.)		A1
	(5x-4)(x-1) = 0			M1
	Notes: attempt to factorise/solve <i>their</i> trinomial quadratic			
	OR		5	
	a correct substitution of <i>their</i> values into a correctly quoted formula			
	OR			
	Completing the square, <i>for their</i> trinomial quadratic, as far as:			
	$(x - \frac{9}{10})^2 - \frac{81}{100} = \frac{-4}{5}$ (o.e.)			
		$x = \frac{4}{5}$ (0.8), 1		A1, A1
				Total 5 marks

Q	Working	Answer	Mark	Notes
4 (a)	$EC = \sqrt{(17)^2 - 5^2}$			M1
	Note: For a trig method, we need to see both stages for M		2	
	to be earned i.e. $\sin \angle FEC = 5/17$ followed by		2	
	$EC = 17 \times \cos(17.1046)$			
		EC = 16.2 (cm)		A1
		(cao)		
(b)	$10 \times (10 + 7 + FB) = "16.248"^2$			M1
	OR			
	OR			
	10(DE) 11.(240112		2	
	$10 \times (BE) = "16.248"^2$		_	
		Accept awrt 9.24, 9.37→9.41		A1
(c)	$7 \times "9.4" = 5 \times FA \text{ (o.e.)}$			M1
		Accept awrt $12.9 \rightarrow 13.2$	2	A1
				Total 6 marks

Question	Wor	king	Answer	Mark	Notes
5 (a)	gf(x) = 2(2 + (5x - 6))	f(-1) = -11			M1
	(=10x-8)			2	
			gf(-1) = -18		A1
(b)	y + 6 = 5x	x = 5y - 6 (o.e.)			M1
			$f^{-1}: x \mapsto \frac{x+6}{5} \text{ (o.e.)}$	2	A1
	Note: For A mark, the inv form	erse must be in the stated	3		
(c)	fg(x) = 5(2(2+x))	-6			M1 oe
	"14+10x"=3(4+2x)			4	M1 dep
	4x = -2 (o.e.)			4	M1 dep
	Note: The correct equation numeric terms gathered. T the same side of the equali	he two terms may be on			
			$x = -\frac{1}{2}$ (o.e.)		A1
					Total 8 marks

Question	Working		Answer	Mark		Notes
6 (a)	$\pi \times 20^2 \times 10$				M1	
			$4000\pi(\mathrm{cm}^3)$	2	A1	cao
	Note: isw					
(b)	Note: Allow a value subst	tituted for π in this part.				
	Vol of spheres = $30 \times \frac{4}{3} \pi R$,3		6	M1	
	_		$=40\pi r^{3}$		A1	
	Note: $40\pi r^3$ could be implied by subsequent method marks [could even be implied by $40r^3$ where π has been cancelled]					
	Total volume =	Increase in volume =			M1	
	$"4000\pi" + "40\pi r^3"$	$20^2 \times \pi \times 6.4 \ (2560\pi)$				
	$(12566.3+125.663r^3)$	(8042.47)				
	$"4000\pi" + "40\pi r^{3}"$ $= \pi \times 20^{2} \times 16.4$ (6560π)	$"40\pi r^3" = 20^2 \times \pi \times 6.4$ (2560\pi)			M1	dep
	$r^3 = 164 - 100$ (or better	•)			M1	dep
	OR Vol of spheres + water = $20 \times 20 \times \pi \times 16.4$ 6560π (20608.8)				OR	
					(M1)	
					(A1)	
	Note: 26240π if $r = 40$ used					
	6560π –" 4000π " (256)	0π, 8042.47)			(M1)	

Volume of one sphere = $\frac{"2560\pi"}{30} \left(\frac{256\pi}{3}\right)$ $40\pi r^3$	="2560π"	(M1	dep)
OR			
$\frac{4}{3}\pi r^3 = \frac{"2560\pi"}{30} \left(\frac{256\pi}{3}\right)$			
$r^3 = 64$		(M1	dep)
Note: Ignore -4 Ignore any prior unrounded value answer $r = 4$ is given		A1	cao
Note: Misread (using radius = 40) loses mark in part (a) and the final A mark. A (including the 2 nd A mark, are available	ll other marks		
			Total 8 marks

Question	Working	Answer	Mark	Notes
7 (a)	$2.3t^2 + 14t^1 + 13$		2	M1 2 terms correct
	$6t^2 + 14t + 13$	3 terms correct (cao)		A1
(b)	" $2\times6t+14$ "			M1 1 term correct
	12t + 14		2	A1 ft
	Note: ft from part (a) provided there are two terms.			
(c)	$"6t^2 + 14t + 13" = "12t + 14"$			M1
		$6t^2 + 2t - 1 (=0)$		A1 cao
	$t = \frac{-2 \pm \sqrt{2^2 - 4 \times 6 \times (-1)}}{2 \times 6}$			M1
	Note: Correct substitution of their a , b and c into formula (must be a trinomial quadratic but NOT " $6t^2 + 14t + 13$ ")		5	
	Note: B mark for evaluation of their discriminant. Only ft if working seen and discriminant is not negative. But, an answer of $t = 0.27$ (or better) implies this ft mark. (see below)	$\sqrt{28}$ or $\sqrt{7}$		B1 ft
	Note: $t = 0.27$ or giving both positiveve & negativeve answers loses the final A mark Do not penalise -0.608 (N/A) or where the negative value is clearly eliminated. No working, but sight of $t = 0.27$ gains 4 out of 5 marks	t = 0.274		A1 awrt 0.274
				Total 9 marks

Qu	estion	Working	Answer	Mark	Notes
	Penalis	e missing labels once only in the question, the first	time it occurs		
8	(a)		A drawn and labelled	1	B1
	(b)	B has coordinates (3, 3), (3, 9), (7, 1)	B drawn and labelled	3	B3 -1eeoo
	(c)	C has coordinates (-3, -3), (-9, -3), (-1, -7)	C drawn and labelled	3	B3ft -1eeoo
	(d)	$ \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} " \begin{pmatrix} -3 & -9 & -1 \\ -3 & -3 & -7 \end{pmatrix} "$			M1
		Diameter (2 2) (2 0) (7 1)	D drawn and labelled	3	A2 -1eeoo
		D has coordinates (3, -3), (3, -9), (7, -1) Note: If matrix product not seen, then it can be implied from a "correct" D.	D drawn and labelled		A2 -1ee00
	(e)	Note: Must be consistent with their diagram Accept $y = 0$ for x-axis	Reflection in x-axis	1	B1
					Total 11 marks

Question	Working		Answer	Mark		Notes
9 (a)	Mean time = $\frac{10 \times (15) + 14}{10}$	$\frac{4 \times (35) + 90 \times (50) +}{200}$	$54 \times (70) + 32 \times (85)$ $\left(=\frac{11640}{200}\right)$			
	Using a correct midpoint in	Using a correct midpoint in a product			M1	
	Attempt to use $\sum \frac{frequence}{c}$	y×midpoint 200			M1	
	Note: Allow for consistent to midpoint i.e. 15.5, 35.5, Allow UCBs or LCBs			4		
	A minimum of 2 term				M1	dep
	Using fully correct $\sum \frac{freq}{}$	200	58 minutes		A1	•
(b)	(b) 5 bars drawn Heig		Heights $\frac{1}{3}$, 1.4, 4.5, 2.7 and 3.2		B5	-1eeoo
	Note: For a height of 1/3 all line drawn between 0.3 and Gap(s) between bars is one of	0.4 inclusive		5		
	SC: If B0 but all correct free calculated Then B1.	quency densities				
(c)		ng frequency sity of 4.5			M1	
	$90 \times \frac{16}{20}$ (72)	5-40)×4.5 (72)			M1	dep
	$10 + 14 + 90 \times \frac{16}{20} (= 96)$	students)		4	M1	dep, all correct
			$\frac{96}{200}$, 0.48, 48% (o.e.)		A1	
						Total 13 marks

Question	(3	1)	Answer	Mark	Notes
10 (a)(i)			$\overrightarrow{AB} = 2\mathbf{b} - 6\mathbf{a}$ (o.e.)		B1
(ii)				4	B1
	6a + "3(2b - 6a)"	2b + 2(2b - 6a)"	$\overrightarrow{OP} = 3\mathbf{a}$	-	M1
(iii)	()				A1
			$\overrightarrow{OC} = 6\mathbf{b} - 12\mathbf{a} \text{ (o.e.)}$		Al
(b)	$\overrightarrow{OQ} = \frac{1}{m} "(6\mathbf{b} - 12\mathbf{a})"$				M1
	$\overrightarrow{PQ} = \overrightarrow{PO} + \overrightarrow{OQ} = -"3\mathbf{a}" + "-$	$\frac{1}{n}(6\mathbf{b}-12\mathbf{a})"$		3	M1 dep
			$\overrightarrow{PQ} = \left(-3 - \frac{12}{m}\right)\mathbf{a} + \left(\frac{6}{m}\right)\mathbf{b}$ \mathbf{OR}		A1
			Accept $-3\mathbf{a} + \frac{1}{m}(6\mathbf{b} - 12\mathbf{a})$		
(c)	$\Delta s \frac{OAC}{OPQ}$ similar Δs			3	M1
	$\frac{OP}{OA} = \frac{OQ}{OC} \left(= \frac{PQ}{AC} \right) = \frac{1}{m} = \frac{1}{2}$				M1
	OR				OR
	$\frac{"\left(-3 - \frac{12}{m}\right)"}{"\left(\frac{6}{m}\right)"} = "\frac{-6}{2}" \text{(o.e.)}$				(M1) oe
	Note: could be in ratio form				
	$-6 - \frac{24}{m} = -\frac{36}{m}$ (o.e.)				(M1 dep)

	OR			OR
	$\overrightarrow{PQ} = "\left(-3 - \frac{12}{m}\right)"\mathbf{a} + "\left(\frac{6}{m}\right)"\mathbf{b} = k\overrightarrow{AB} = k\left("-6\mathbf{a} + 2\mathbf{b}"\right)$			(M1) oe
	Equating coefficients of a and b			(M1 dep)
	Note: Using $\overrightarrow{PQ} = \overrightarrow{AC}$ instead of being parallel goes nowhere and commonly arrives at $m = 1$			
	Note : $m = 2$, no incorrect working seen \Rightarrow full marks	m=2		A1
(d)	Note: ft from (b) and/or (c) Does not need to be simplified	$\overrightarrow{PQ} = -9\mathbf{a} + 3\mathbf{b}$	1	B1 ft
(e)	Note: Using /seeing $\left(\frac{1}{"m"}\right)^2$ or $\left(\frac{1}{2}\right)^2$ Do not accept $m=1$	$\left(\frac{1}{"m"}\right)^2 OR \left(\frac{1}{2}\right)^2$	3	B1 ft
	Area of $\triangle OPQ = \left(\frac{1}{"m"}\right)^2 \times 12$			M1
		Area of $PQAC = 9 \text{ cm}^2$		A1
				Total 14 marks

Questi	on	Working	Answer	Mark		Notes
11	(a)		-2.8	3	B1	
			-4.6		B1	
		Note: Accept awrt these values – do not penalise incorrect	-0.4		B1	
		rounding in this question				
	(b)	Notes: ft from their table values Accuracy: ±1 small square If a point is not plotted, it can be inferred from their curve passing through (within tolerance) the required point.	Curve drawn	3	B3	-1 mark for straight line segments each point missed each missed segment each point not plotted each point incorrectly plotted tramlines very poor curve
	(c)		-5.5 +/- 1 small square	1	B1	ft
	(d)	Correct tangent drawn and attempting $\frac{\Delta y}{\Delta x}$ from curve Note: Tangent must touch curve at $x = 3$. An attempt at $\frac{\Delta y}{\Delta x}$ seen. If this M not earned, then no A mark (i.e. calculus alone		2	M1	
		earns no marks)				
		accept gradient values in the range $3.8 - 4.4$		4	A1	
	(e)		$\frac{x^3}{6} - \frac{x}{4} + \frac{5}{x^2} - 4 = 0 \iff \frac{x^3}{6} + \frac{5}{x^2} - 8 = \frac{x}{4} - 4$ The correct line identified (or drawn) earns method irrespective of working		M1	

		drawn $y = \frac{x}{4} - 4$		A1
	Notes: Ignore missing label	4		
	The line must pass through $(0, -4)$ and $(4, -3)$ (within			
1	tolerance) – extrapolate if necessary			
	, <u>, , , , , , , , , , , , , , , , , , </u>	1.1 +/- 1 small		A1 ft (ft dep on 1 st A1)
		square,		A1 ft (ft dep on 1 st A1)
	Note: ft from the correct straight line and their curve (ignore	2.9 +/- 1 small		in the (in step on 1 111)
	values of y)	square		
(f)	3 - 3 -	square	3	M1
	$\frac{x^3}{6} + \frac{5}{x^2} - 2 = 0$ rearranged as $\frac{x^3}{6} + \frac{5}{x^2} - 8 = -6$		3	IVII
		y = -6 drawn (or		A1
		implied)		
	OR	impried)		OR
				(M1)
	statement that $y = \frac{x^3}{6} + \frac{5}{x^2} - 2$ is obtained by moving $y = \frac{x^3}{6} + \frac{5}{x^2} - 8 \qquad 6 \text{ units up the } y\text{-axis}$ $\therefore y = \frac{x^3}{6} + \frac{5}{x^2} - 2 \text{ will not intersect the } x\text{-axis since minimum is now } y = 0.5$			(IVII)
				(A1)
		correct conclusion drawn		A1
	Note: " and therefore has no solutions"			
	Final mark can only be awarded if the previous M and A			
	are awarded.			
				Total 16 marks